

❖ Algorithm Reference sheet

Algorithm 1 Period Finding

- 1: Start with $|0 \dots 0\rangle |0 \dots 0\rangle$ (We refer to these as first and second register, each have n qubits)
 - 2: Apply $H^{\otimes n}$ on the first register to get $\frac{1}{\sqrt{N}} \sum_{y=0}^{N-1} |y\rangle |0\rangle$
 - 3: Apply U_f
 - 4: Measure the 2nd register.
 - 5: Ignore the 2nd register and apply QFT_N to the 1st register.
 - 6: Measure the 1st register to get value a .
 - 7: Postprocessing: Use a and N to find k and r .
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Algorithm 2 Factoring

- 1: Pick x at random from $\{2, \dots, M-1\}$
 - 2: **if** $\gcd(x, M) \neq 1$ **then**
 - 3: $\gcd(x, M)$ is a non-trivial factor of M so we are done!
 - 4: **else**
 - 5: Use quantum Period Finding algorithm (alg 1) to find smallest s such that $x^s = 1 \pmod{M}$.
 - 6: Call this variable r .
 - 7: **if** r is odd **then**
 - 8: Start over..
 - 9: **else if** $x^{r/2} = \pm 1 \pmod{M}$ **then**
 - 10: Start over..
 - 11: **else**
 - 12: $x^{r/2} \pmod{M}$ is a non-trivial square root of 1 mod M
 - 13: **end if**
 - 14: **end if**
 - 15: Postprocessing: Compute $\gcd(x^{r/2} - 1, M)$ and $\gcd(x^{r/2} + 1, M)$ to find the factors of M .
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